

## Extra Practice problems #1

1. Convert the complex number  $z = \frac{2i}{e^{1+i}}$  to polar form and to cartesian form.
2. Let  $f(z) = \frac{z^2}{|z^2|}$ . Does  $f$  have a limit as  $z \rightarrow 0$ ?
3. (a) Solve for  $z$ :  $iz = 4 - iz$ .  
(b) Evaluate  $\text{Arg} \left( \frac{i}{-2-2i} \right)$   
(c) Find all distinct values of  $(1 - \sqrt{3}i)^{1/3}$   
(d) Evaluate  $\left( \frac{1}{1+i} \right)^{10}$ .
4. Find the solutions of  $\cos z = 2i$ .
5. If  $u$  and  $v$  are harmonic conjugates, is the product  $uv$  always harmonic?
6. Use the definition of  $\sin z$  and  $\cos z$  to derive the identity  $\sin^2 z + \cos^2 z = 1$ .
7. Let  $f(z) = (1 + e^z)^{-1}$ .  
(a) Find the domain and range of  $f$ .  
(b) Where is  $f$  analytic?
8. Use the rigorous definition of limits to show that the function  $f(z) = \bar{z}$  is continuous on the whole complex plane.