

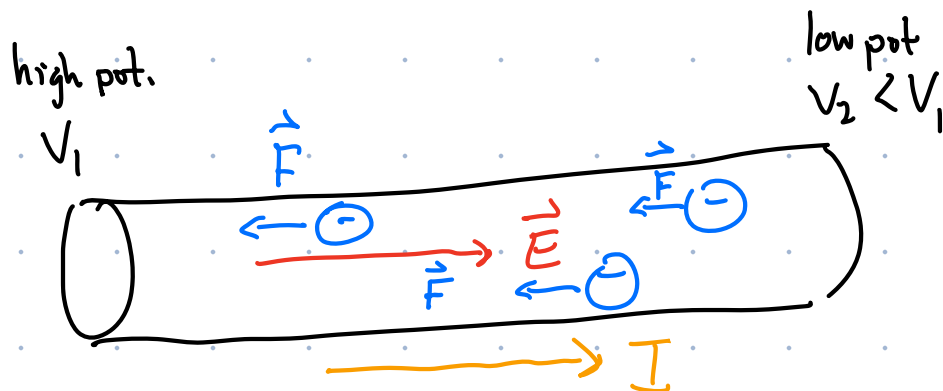
Jake Bobowski

SCI 266

jake.bobowski@ubc.ca

<https://cmps-people.ok.ubc.ca/jbobowsk/phys231.html>

Consider a conductor w/ a pot. diff ΔV across it.



Recall that $\vec{E}$ point from high to low pot./volt.

Cross conductor from left to right.

$$V_2 - V_1 < 0 \text{ (negative)}$$

Get a negative change in voltage when cross conductor in dir'n of I

In this case, $\Delta V = V_2 - V_1 = -IR$
 $\uparrow$ resistance.

Cross conductor from right to left.

$$V_1 - V_2 > 0 \text{ (positive)}$$

Get a positive change in volt. when cross conductor anti-parallel to I

$$\Delta V' = V_1 - V_2 = +IR$$

Relationship between electric field $\vec{E}$ and volt. differences.

$$\Delta V = - \int_1^2 \vec{E} \cdot d\vec{l}$$

To see the origins of this relationship, mult. both sides by charge q of pt. charge.

$$q \Delta V = - \int_1^2 (q \vec{E}) \cdot d\vec{l}$$

$\underbrace{\hspace{1cm}} \quad \underbrace{\hspace{1cm}}$
 $\Delta U = -\Delta K$ $\vec{F}$

change in P.E.

$\vec{E}$ -force is conservative. $\therefore$ Mechanical energy is conserved

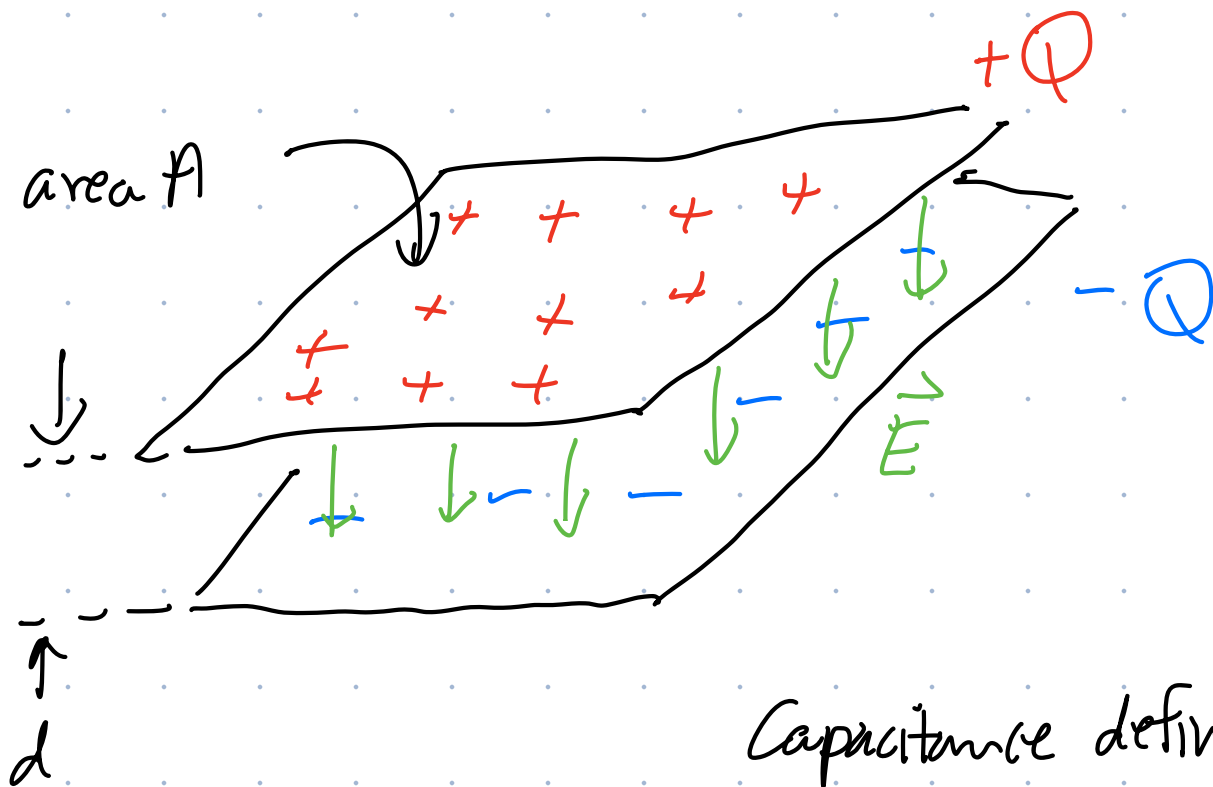
$$\Delta U + \Delta K = 0$$

$$\Rightarrow \Delta U = -\Delta K$$

$$\therefore \Delta K = \int_1^2 \vec{F} \cdot d\vec{l}$$

Work-K.E. Theorem.

Parallel Plate Capacitor



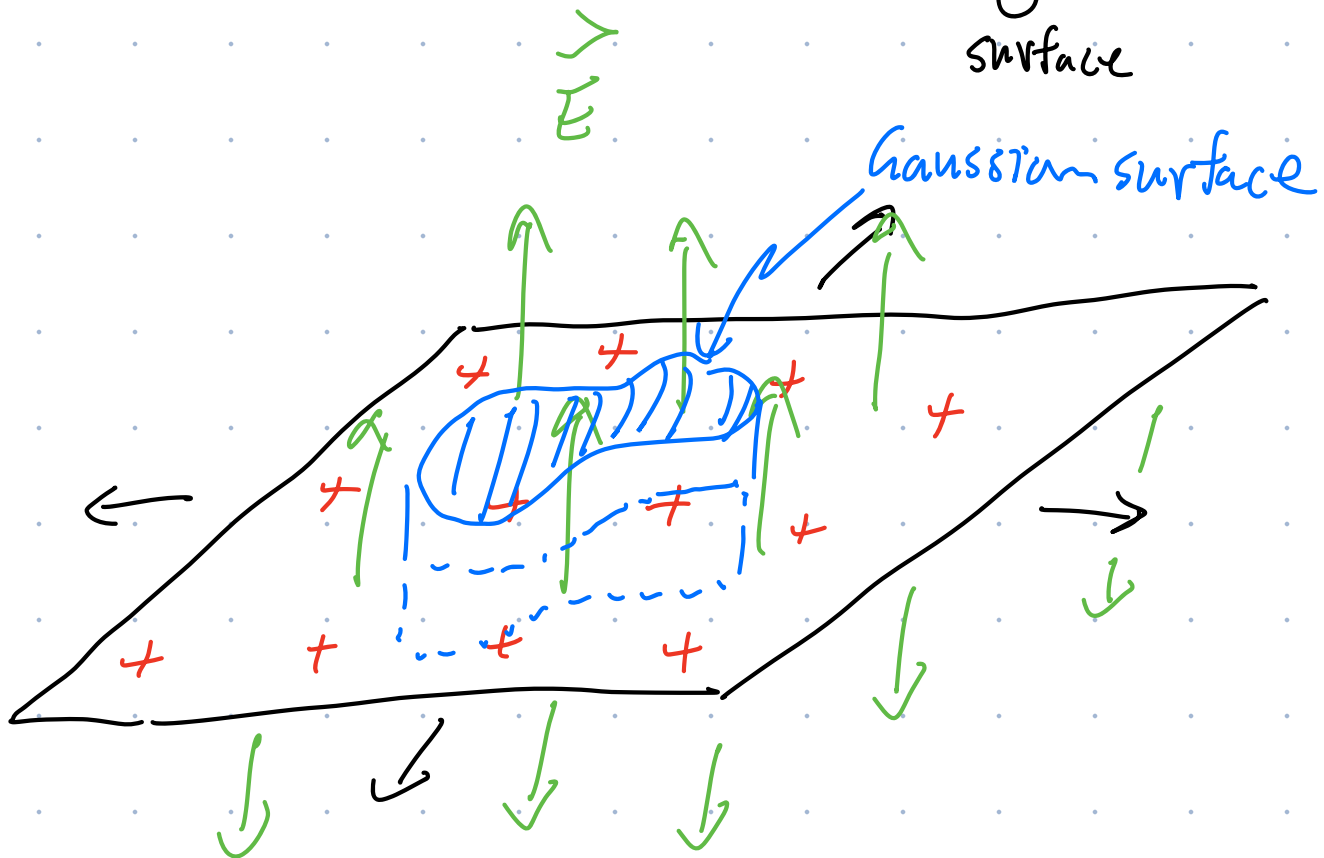
Capacitance defined to be

$$C = \frac{Q}{|\Delta V|}$$

- ① calc. $\vec{E}$ between plates
- ② calc. $\Delta V = -\int \vec{E} \cdot d\vec{l}$ from one plate to the other
- ③ Find $C = \frac{Q}{|\Delta V|}$

We can find $\vec{E}$ of a large uniformly charged plate using Gauss's law :

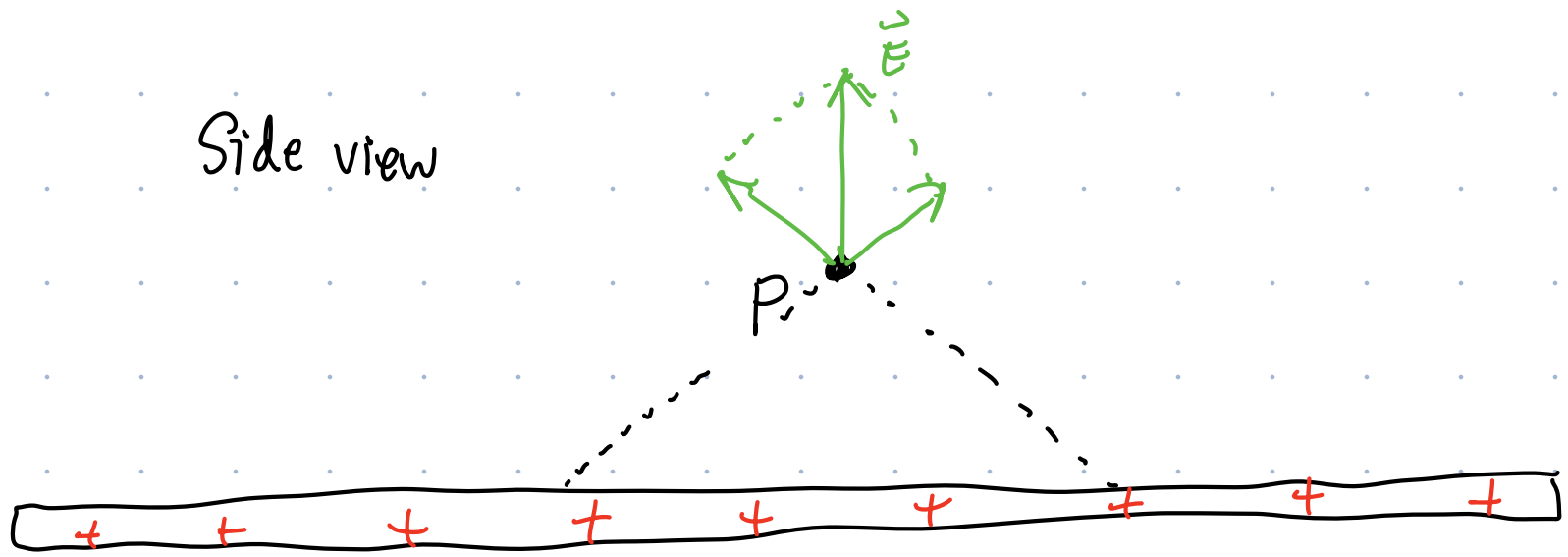
$$\oint_{\text{surface}} \vec{E} \cdot d\vec{A} = \frac{q_{\text{enc}}}{\epsilon_0}$$



$$\text{Find } E = \frac{\sigma}{2\epsilon_0}$$

for a uniformly charge surface.
where σ is the charge
per unit area : $\sigma = \frac{Q}{A}$.

Side view



By symmetry, for points close to large charged surface, $\vec{E}$ will always be $\perp$ to surface.