

Learning Analytics

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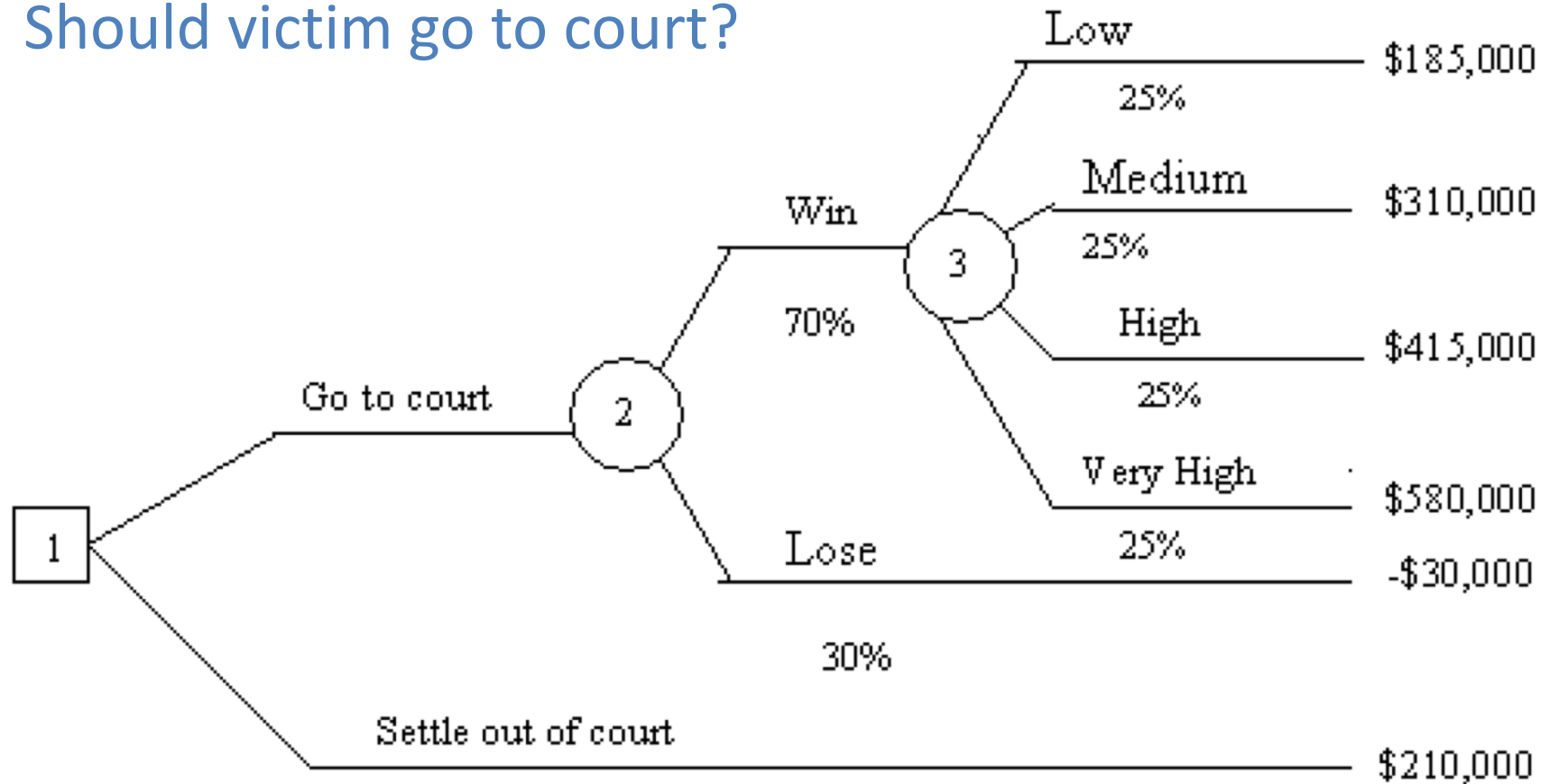
Computer Science

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DECISION TREE

POSSIBLE OUTCOMES OF DECISION TO SETTLE OR GO TO COURT

Should victim go to court?



Decision



Uncertainty

General Decision Making Problem

- Consider an intelligent tutoring system designed to assist the user in programming
- Possible actions (intended to be helpful)?

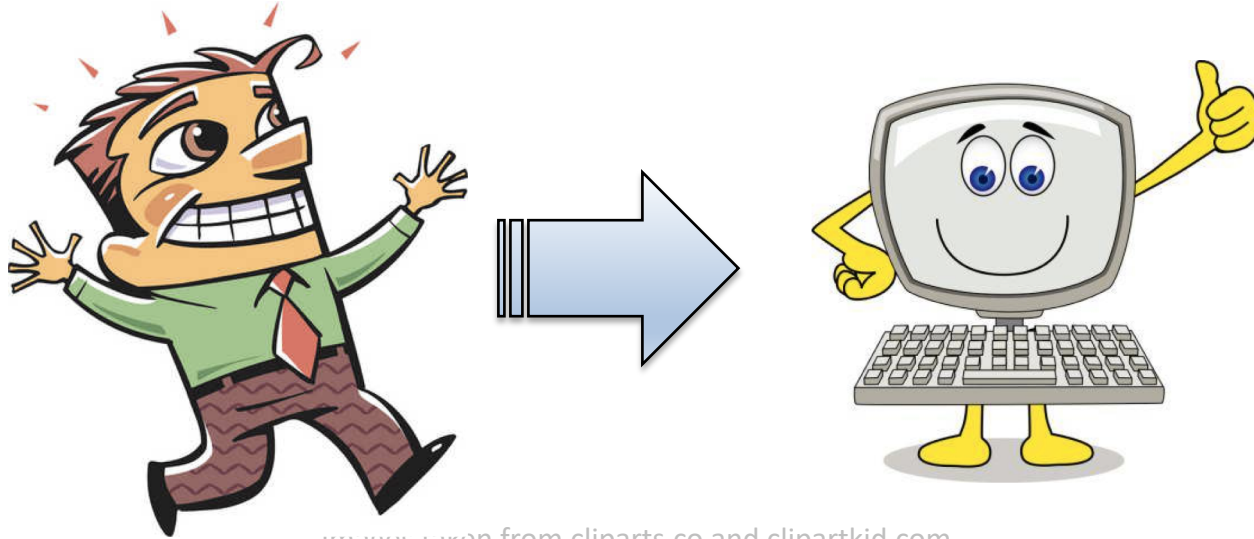
General Decision Making Problem

- Consider an intelligent tutoring system designed to assist the user in programming
- Possible actions (intended to be helpful):
 - A1: Auto-complete the current programming statement
 - A2: Suggest several options for completing the current statement
 - A3: Provide hints for completing the statement
 - A4: Ask if user needs help in a pop-up dialogue
 - ...
 - A5: Keep observing the user (do nothing)

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- What system does should depend on helpful it can be for the user

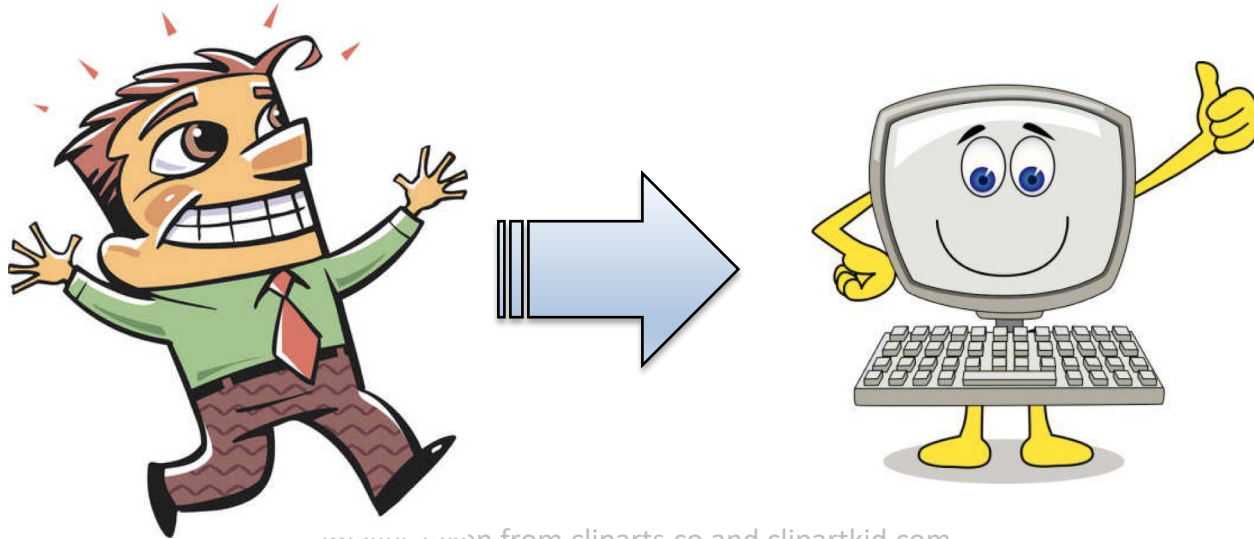
“Your Happiness is My Happiness”



images taken from cliparts.co and clipartkid.com

- System acts to help user
- If user is happy, system is doing the right thing

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- System acts to help user
- If user is happy, system is doing the right thing
- Therefore:
 - System makes actions to keep user happy
 - **Utility function** should reflect user’s preferences

Utility Function with User Variables

- System's decision problem:
 - Which is the best action to make user most happy?
 - With consideration to how much help the user needs right now

Utility Function with User Variables

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- $EU(\text{Action}) = \text{Pr}(\text{Help}) \times U(\text{Help}, \text{Action})$

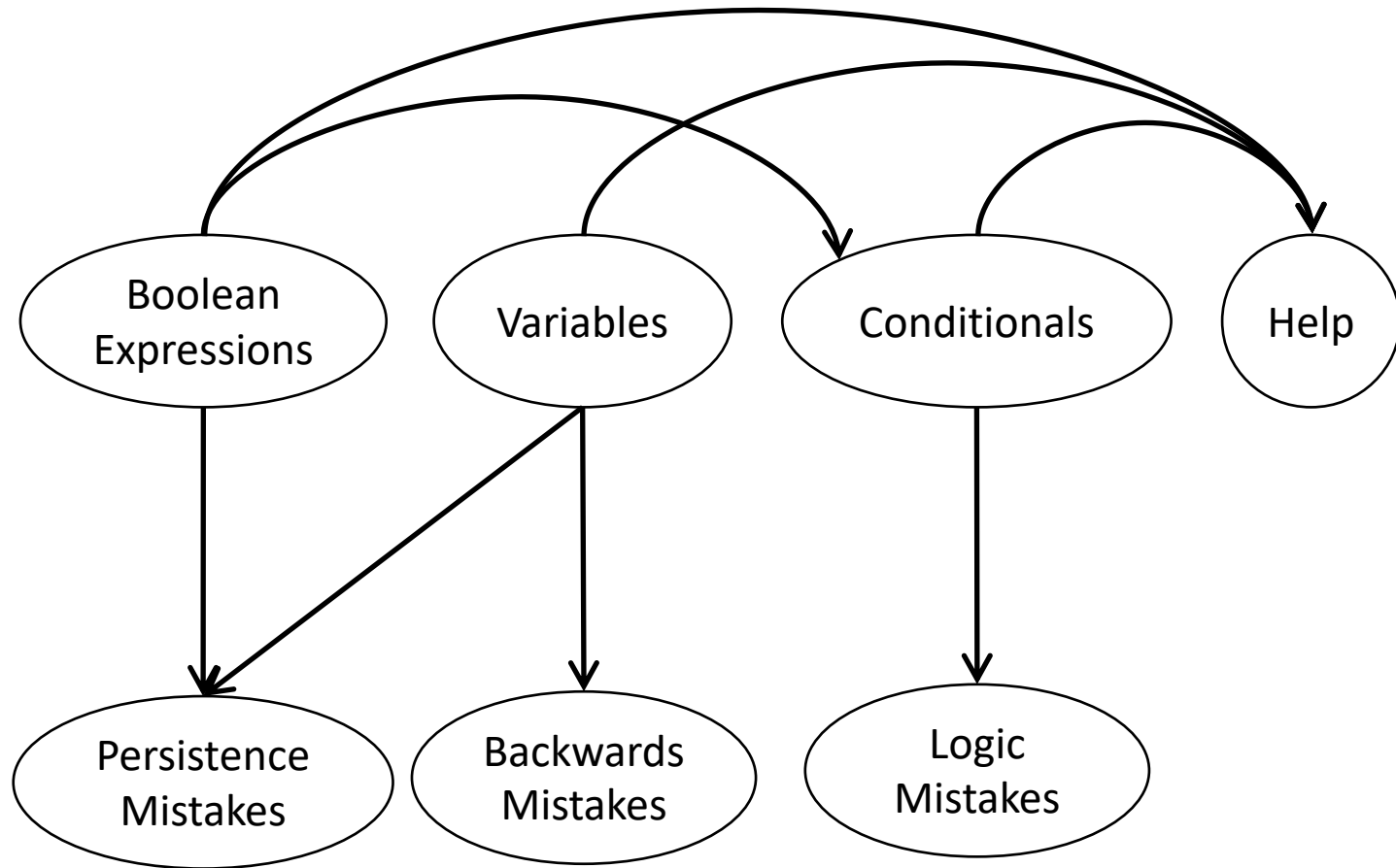
Comes from marginal distribution
computed from Bayes net



Comes from utility
defined/elicited and
stored in separate file



Possible Way to Compute $\text{Pr}(\text{Help})$



We will come back to this...

Defining $U(\text{Help}, \text{Action})$

- For each scenario, assign real number to each action: auto-complete, suggest options, hint, ask, do nothing
- If Help is high,
 - Auto-complete, Suggest options, Hint are more appropriate
 - Note: Should also model quality of suggestion
- If Help is medium,
 - Ask and Hint is more appropriate
- If Help is low,
 - Do nothing is more appropriate

Example: $U(\text{Help}, \text{Action})$

- Define U in $[-10, +10]$
 - Best outcome gets +10
 - Worst outcome gets -10
- Case: When Help is low, Do nothing is best
 - $U(1, 5) = 10$
 - $U(1, 4) = -10$ % pop-up dialogue, super annoying
 - $U(1, 3) = -5$ % hint, somewhat disruptive
 - $U(1, 2) = -7$ % suggest, somewhat disruptive
 - $U(1, 1) = -2$ % auto-complete, not too intrusive if easy to ignore
- Case: When Help is high, Auto-complete, Suggest options, Hint are best
 - $U(3, 1) = 10$ % auto-complete
 - $U(3, 2) = 8$ % suggest, still helpful when stuck
 - etc.
- Case: When Help is medium, Ask and Hint are most appropriate
 - $U(2, 1) = -5$ % auto-complete, not as great

Finally, we can do something

- Computing $\Pr(\dots)$ is like doing only categorization
- Now we can start making decisions



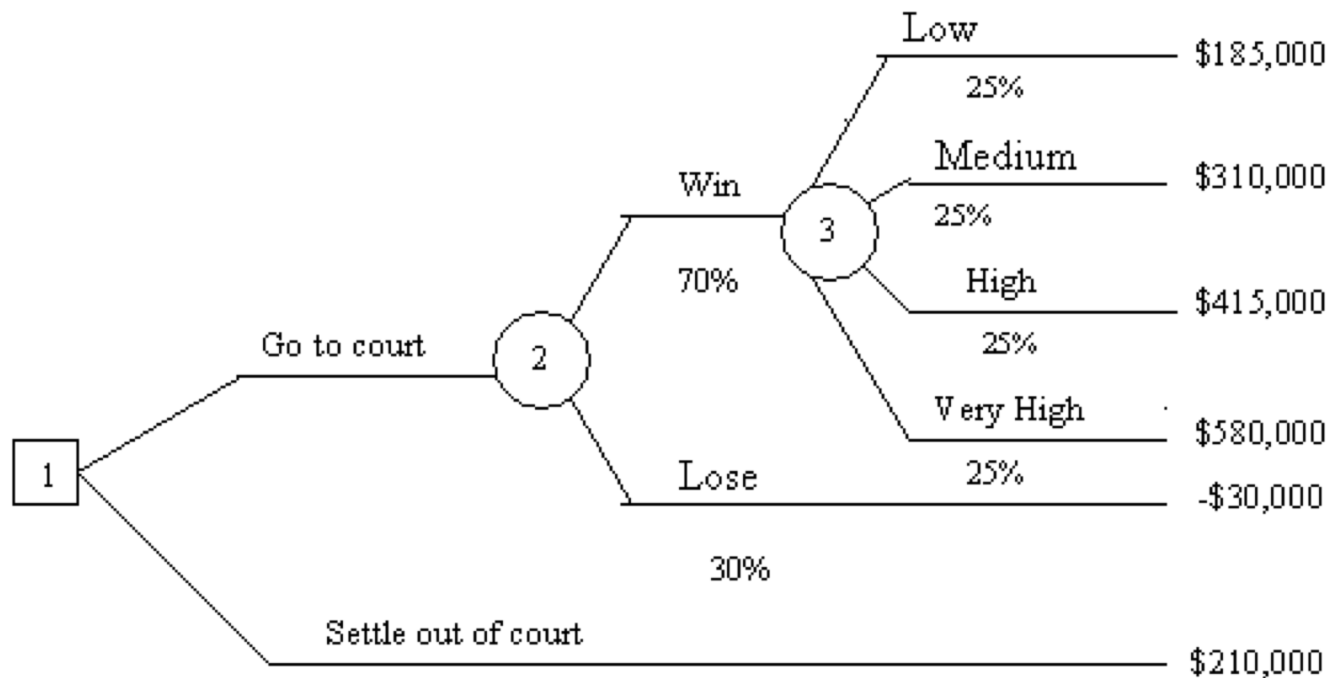
What to do with our Beliefs?


- Given our belief of the world, $\Pr(\mathbf{X}|\mathbf{E})$, we want to see what action is best
 - Uses **probability theory**
- Need to quantify how good an action is with respect to each possible state defined by \mathbf{X}
 - Uses **utility theory**


Decision Making Example

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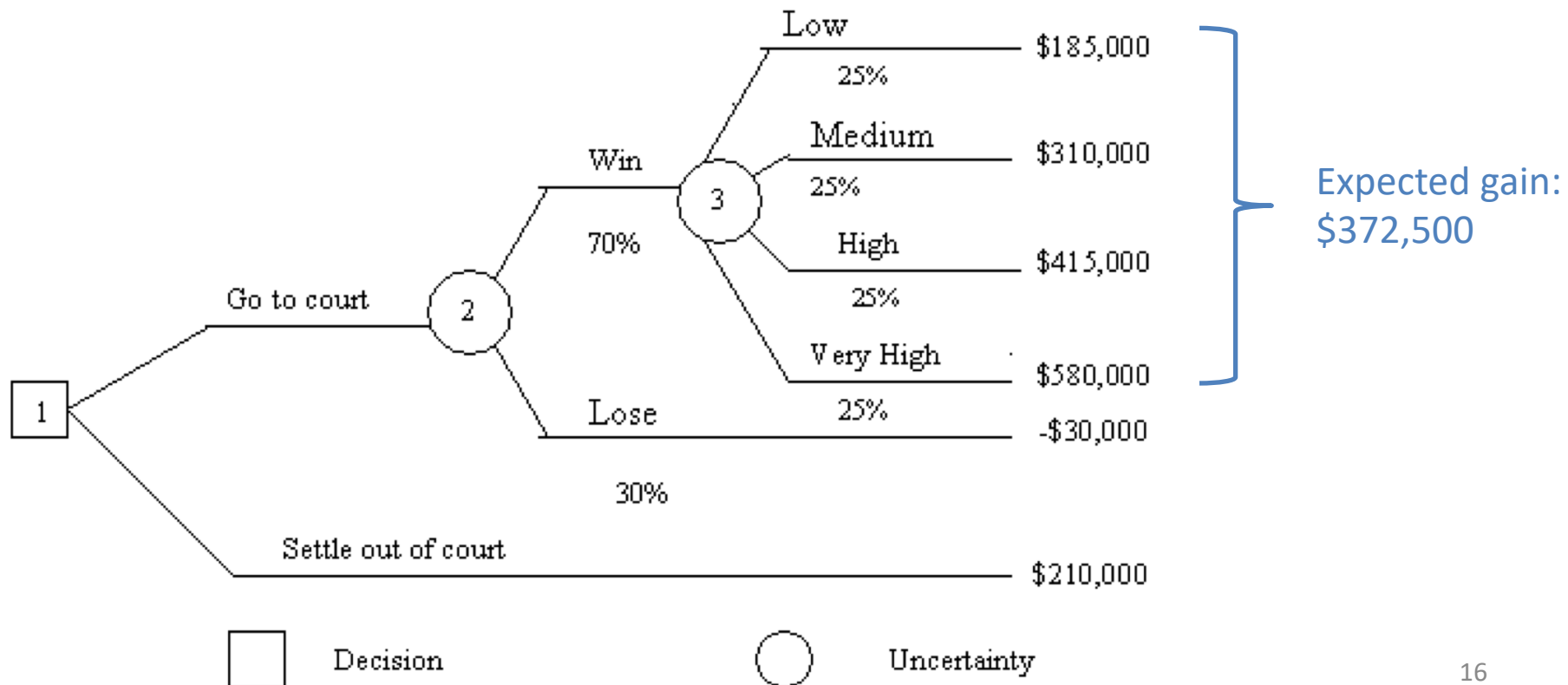
 Decision

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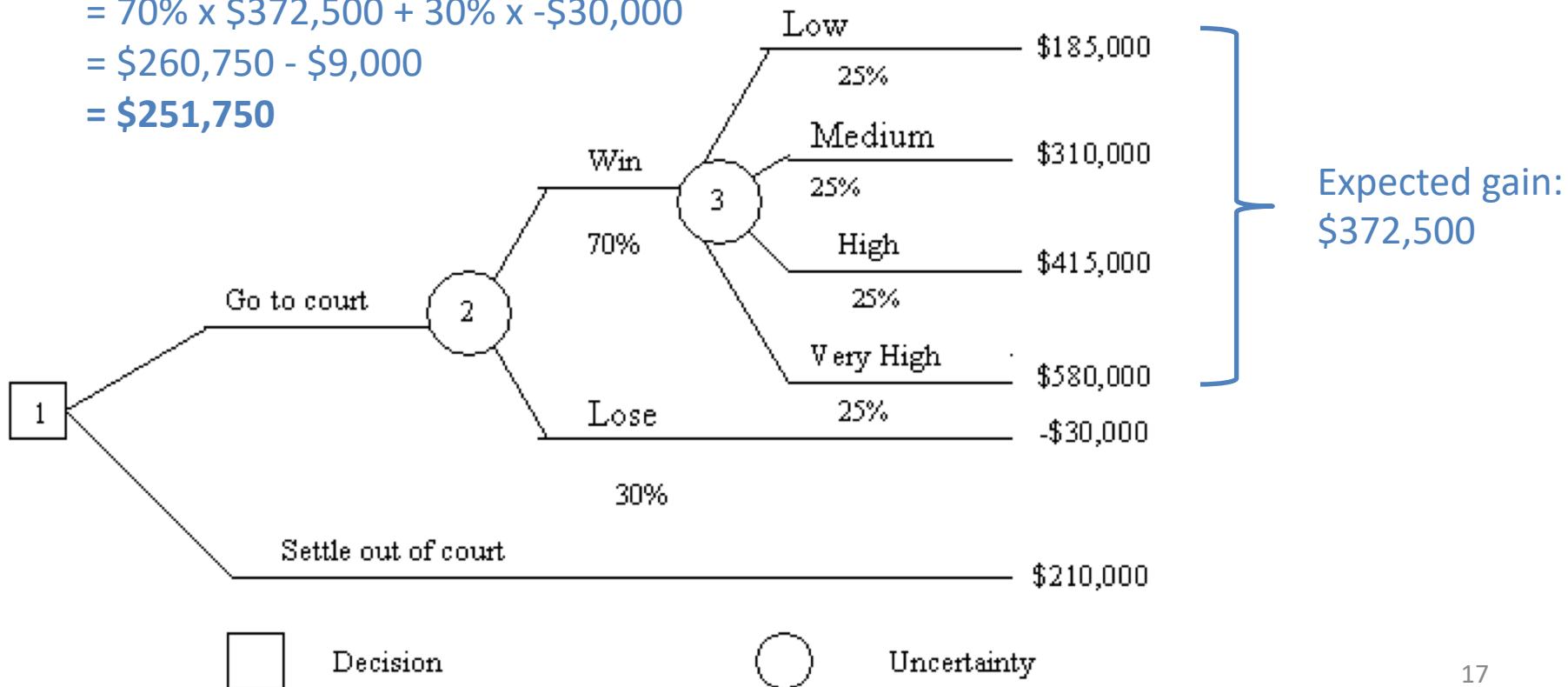
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Decision Making Example

DECISION TREE
 POSSIBLE OUTCOMES OF DECISION TO SETTLE
 OR GO TO COURT

Expected value of going to court
 = $70\% \times \$372,500 + 30\% \times -\$30,000$
 = $\$260,750 - \$9,000$
 = **$\$251,750$**



Example

- You want to take a morning walk but not sure if you should bring an umbrella
- You don't really want to carry an umbrella
- But it looks like it may rain and you don't want to get wet

- Possible actions: bring umbrella, leave it at home

- How do you decide what to do?

Decision Making

- How much do you like being wet vs. dry?
- How much do you like having to carry an umbrella around?
- You have a set of preferences over the alternatives
 - E.g.: not having to carry umbrella and staying dry, is better than carrying umbrella and staying dry, is better than ...

Example: Decision Scenarios

		States	
		It rains	It doesn't rain
Actions	Take umbrella	Encumbered, Dry	Encumbered, Dry
	Leave umbrella	Wet	Free, Dry

- 2 states x 2 actions = 4 possible outcomes

Example: Decision Scenarios

		States	
		It rains	It doesn't rain
Actions	Take umbrella	Encumbered, Dry +7	Encumbered, Dry +5
	Leave umbrella	Wet -8	Free, Dry +10

- 2 states x 2 actions = 4 possible outcomes
- Utility = a real number value of each outcome

Example: Decision Scenarios

		States	
		It rains 0.4	It doesn't rain 0.6
Actions	Take umbrella	Encumbered, Dry +7	Encumbered, Dry +5
	Leave umbrella	Wet -8	Free, Dry +10

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- $$\begin{aligned} EU(\text{takeUmb}) &= \text{Pr}(\text{rain})U(\text{encDry}) + \text{Pr}(\text{noRain})U(\text{encDry}) \\ &= (0.4)(7) + (0.6)(5) = 5.8 \end{aligned}$$

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- 2 states x 2 actions = 4 possible outcomes
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- $$EU(\text{leaveUmb}) = \text{Pr}(\text{rain})U(\text{wet}) + \text{Pr}(\text{noRain})U(\text{freeDry})$$
$$= (0.4)(-8) + (0.6)(10) = 2.8$$

Example: Decision Scenarios

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- $EU(\text{takeUmb}) = 5.8$
- $EU(\text{leaveUmb}) = 2.8$
- Which action will you choose?

Key Ideas

- Main concepts
 - Probability theory enables us to estimate beliefs of the world
 - Utility theory enables us to express the strength of our preferences over outcomes
 - Decision making problems require both
- Representation:
 - Decision making under uncertainty:
 - Probability distribution of outcomes
 - Utility function to express preference of outcomes